

B.Sc.- III (CBCS Pattern) Semester-VI
021C - (DSE-V) Mathematics Paper-I : Numerical Methods

P. Pages : 2

Time : Three Hours



GUG/S/25/13363

Max. Marks : 60

- Notes : 1. Solve all **five** questions.
2. All questions carry equal marks.

UNIT – I

1. a) Find the root of the equation $e^{-x} - x = 0$ by the secant method in four iterations. The initial estimates are $x_1 = 0, x_2 = 1$ **6**
- b) Prove that the rate of convergence of the N-R method is 2 and is given by **6**
- $$|e_{n+1}| = \left| -\frac{f''(r)}{2f'(r)} \right| |e_n|^2$$
- where r is the exact root of the equation $f(x) = 0$.

OR

- c) Solve the system of equations. **6**
- $$0x_1 + 2x_2 - 3x_3 = 1, 3x_1 - x_2 + x_3 = 8, 2x_1 + x_2 - 2x_3 = 6$$
- by the Gauss elimination method with partial pivoting.
- d) Use Gauss-Jordon method to solve the system **6**
- $$x + y + z = 6, 2x - 3y + 4z = 1, 3x + 4y + 5z = 25.$$

UNIT – II

2. a) Compute y_4 if $y = f(x)$ be a polynomial of degree three such that **6**
- $$y_2 + y_6 = 578 \text{ and } y_3 + y_5 = 470.$$
- b) Express the polynomial $f(x) = 3x^2 - 5x + 7$ into factorial polynomial and obtained their forward differences. **6**

OR

- c) Use Newton-Gregory backward interpolation formula to find a cubic polynomial from the data: **6**

x :	0	1	2	3	4	5
y :	1	3	7	13	21	31

- d) Using Lagrange interpolation formula, express **6**
- $$\frac{3x^2 - 8x + 13}{(x+1)(x-2)(x-3)} \text{ as sum of partial fractions.}$$

UNIT – III

3. a) The distance covered by an athlete for the 40 meters is given by the following values: 6
- | | | | | | | |
|---------------|---|---|----|----|----|----|
| t(sec) : | 0 | 1 | 2 | 3 | 4 | 5 |
| s(distance) : | 0 | 4 | 11 | 19 | 28 | 40 |

Find the speed of the athlete at $t = 4.8$ sec.

- b) Find the first derivative of the function $f(x)$ at $x = 1$ from the give data: 6
- | | | | | | | |
|--------------|---|---|----|----|-----|-----|
| x : | 0 | 1 | 2 | 3 | 4 | 5 |
| $y = f(x)$: | 2 | 9 | 28 | 65 | 126 | 217 |

OR

- c) Discuss maxima and minima of the function $y = f(x)$ specified by the values : 6
- | | | | | |
|--------------|----|---|---|-----|
| x : | -2 | 0 | 2 | 4 |
| $y = f(x)$: | -1 | 1 | 3 | 53. |
- d) Find $y'(3)$ from the Lagrange interpolation formula for the function given by the values: 6
- | | | | | |
|--------------|---|---|----|----|
| x : | 3 | 5 | 7 | 9 |
| $y = f(x)$: | 5 | 8 | 12 | 17 |

UNIT - IV

4. a) Derive the Simpson's one-third rule from Newton-Cotes quadrature formula. 6
- b) Evaluate the integral $\int_{0.1}^{0.2} \frac{x^2}{1+x^3} dx$ by the trapezoidal rule. 6

OR

- c) Obtain the Boole's quadrature rule from Newton-Cotes formula. 6
- d) Evaluate the integral $\int_0^3 \frac{dx}{1+x^3}$ by Simpson three-eighth quadrature formula. 6

5. Solve any six

- a) Show that the Newton – Raphson iteration for determining a square root of A has the form. 2
- $$x_{n+1} = \frac{1}{2} \left(x_n + \frac{A}{x_n} \right)$$
- b) Define upper and lower triangular matrix. 2
- c) If h is the interval of differencing, then prove that $E = e^{hD}$. 2
- d) Prove that $\delta = E^{\frac{1}{2}} - E^{-\frac{1}{2}}$. 2
- e) Write the special Newton backward formula for first derivatives at tabular points near $x = x_n$. 2
- f) Write the Newton divided difference formula for second derivatives. 2
- g) Define a truncation error. 2
- h) Define an error constant. 2
